1. Which of the following numbers is a perfect square?
(A) $4^{4} 5^{5} 6^{6}$
(B) $4^{4} 5^{6} 6^{5}$
(C) $4^{5} 5^{4} 6^{6}$
(D) $4^{6} 5^{4} 6^{5}$
(E) $4^{6} 5^{5} 6^{4}$
2. The function $f$ is given by the table

| $x$ | 1 | 2 | 3 | 4 | 5 |
| :---: | :--- | :--- | :--- | :--- | :--- |
| $f(x)$ | 4 | 1 | 3 | 5 | 2 |

If $u_{0}=4$ and $u_{n+1}=f\left(u_{n}\right)$ for $n \geq 0$, find $u_{2002}$.
(A) 1
(B) 2
(C) 3
(D) 4
(E) 5
3. The dimensions of a rectangular box in inches are all positive integers and the volume of the box is $2002 \mathrm{in}^{3}$. Find the minimum possible sum in inches of the three dimensions.
(A) 36
(B) 38
(C) 42
(D) 44
(E) 92
4. Let $a$ and $b$ be distinct real numbers for which

$$
\frac{a}{b}+\frac{a+10 b}{b+10 a}=2
$$

Find $\frac{a}{b}$.
(A) 0.4
(B) 0.5
(C) 0.6
(D) 0.7
(E) 0.8
5. For how many positive integers $m$ is

$$
\frac{2002}{m^{2}-2}
$$

a positive integer?
(A) one
(B) two
(C) three
(D) four
(E) more than four
6. Participation in the local soccer league this year is $10 \%$ higher than last year. The number of males increased by $5 \%$ and the number of females increased by $20 \%$. What fraction of the soccer league is now female?
(A) $\frac{1}{3}$
(B) $\frac{4}{11}$
(C) $\frac{2}{5}$
(D) $\frac{4}{9}$
(E) $\frac{1}{2}$
7. How many three-digit numbers have at least one 2 and at least one 3 ?
(A) 52
(B) 54
(C) 56
(D) 58
(E) 60
8. Let $A B$ be a segment of length 26 , and let points $C$ and $D$ be located on $A B$ such that $A C=1$ and $A D=8$. Let $E$ and $F$ be points on one of the semicircles with diameter $A B$ for which $E C$ and $F D$ are perpendicular to $A B$. Find $E F$.
(A) 5
(B) $5 \sqrt{2}$
(C) 7
(D) $7 \sqrt{2}$
(E) 12
9. Two walls and the ceiling of a room meet at right angles at point $P$. A fly is in the air one meter from one wall, eight meters from the other wall, and nine meters from point $P$. How many meters is the fly from the ceiling?
(A) $\sqrt{13}$
(B) $\sqrt{14}$
(C) $\sqrt{15}$
(D) 4
(E) $\sqrt{17}$
10. Let $f_{n}(x)=\sin ^{n} x+\cos ^{n} x$. For how many $x$ in $[0, \pi]$ is it true that

$$
6 f_{4}(x)-4 f_{6}(x)=2 f_{2}(x) ?
$$

(A) 2
(B) 4
(C) 6
(D) 8
(E) more than 8
11. Let $t_{n}=\frac{n(n+1)}{2}$ be the $n$th triangular number. Find

$$
\frac{1}{t_{1}}+\frac{1}{t_{2}}+\frac{1}{t_{3}}+\ldots+\frac{1}{t_{2002}}
$$

(A) $\frac{4003}{2003}$
(B) $\frac{2001}{1001}$
(C) $\frac{4004}{2003}$
(D) $\frac{4001}{2001}$
(E) 2
12. For how many positive integers $n$ is $n^{3}-8 n^{2}+20 n-13$ a prime number?
(A) one
(B) two
(C) three
(D) four
(E) more than four
13. What is the maximum value of $n$ for which there is a set of distinct positive integers $k_{1}, k_{2}, \ldots, k_{n}$ for which

$$
k_{1}^{2}+k_{2}^{2}+\ldots+k_{n}^{2}=2002
$$

(A) 14
(B) 15
(C) 16
(D) 17
(E) 18
14. Find $i+2 i^{2}+3 i^{3}+\ldots+2002 i^{2002}$.
(A) $-999+1002 i$
(B) $-1002+999 i$
(C) $-1001+1000 i$
(D) $-1002+1001 i$
(E) $i$
15. There are 1001 red marbles and 1001 black marbles in a box. Let $P_{s}$ be the probability that two marbles drawn at random from the box are the same color, and let $P_{d}$ be the probability that they are different colors. Find $\left|P_{s}-P_{d}\right|$.
(A) 0
(B) $\frac{1}{2002}$
(C) $\frac{1}{2001}$
(D) $\frac{2}{2001}$
(E) $\frac{1}{1000}$
16. The altitudes of a triangle are 12,15 , and 20 . The largest angle in this triangle is
(A) $72^{\circ}$
(B) $75^{\circ}$
(C) $90^{\circ}$
(D) $108^{\circ}$
(E) $120^{\circ}$
17. Let $f(x)=\sqrt{\sin ^{4} x+4 \cos ^{2} x}-\sqrt{\cos ^{4} x+4 \sin ^{2} x}$. An equivalent form of $f(x)$ is
(A) $1-\sqrt{2} \sin x$
(B) $-1+\sqrt{2} \cos x$
(C) $\cos \frac{x}{2}-\sin \frac{x}{2}$
(D) $\cos x-\sin x$
(E) $\cos 2 x$
18. If $a, b, c$ are real numbers such that $a^{2}+2 b=7, b^{2}+4 c=-7$, and $c^{2}+6 a=-14$, find $a^{2}+b^{2}+c^{2}$.
(A) 14
(B) 21
(C) 28
(D) 35
(E) 49
19. In quadrilateral $A B C D, m \angle B=m \angle C=120^{\circ}, A B=3, B C=4$, and $C D=5$. Find the area of $A B C D$.
(A) 15
(B) $9 \sqrt{3}$
(C) $\frac{45 \sqrt{3}}{4}$
(D) $\frac{47 \sqrt{3}}{4}$
(E) $15 \sqrt{3}$
20. Let $f$ be a real-valued function such that

$$
f(x)+2 f\left(\frac{2002}{x}\right)=3 x
$$

for all $x>0$. Find $f(2)$.
(A) 1000
(B) 2000
(C) 3000
(D) 4000
(E) 6000
21. Let $a$ and $b$ be real numbers greater than 1 for which there exists a positive real number $c$, different from 1 , such that

$$
2\left(\log _{a} c+\log _{b} c\right)=9 \log _{a b} c
$$

Find the largest possible value of $\log _{a} b$.
(A) $\sqrt{2}$
(B) $\sqrt{3}$
(C) 2
(D) $\sqrt{6}$
(E) 3
22. Under the new AMC 10, 12 scoring method, 6 points are given for each correct answer, 2.5 points are given for each unanswered question, and no points are given for an incorrect answer. Some of the possible scores between 0 and 150 can be obtained in only one way, for example, the only way to obtain a score of 146.5 is to have 24 correct answers and one unanswered question. Some scores can be obtained in exactly two ways; for example, a score of 104.5 can be obtained with 17 correct answers, 1 unanswered question, and 7 incorrect, and also with 12 correct answers and 13 unanswered questions. There are (three) scores that can be obtained in exactly three ways. What is their sum?
(A) 175
(B) 179.5
(C) 182
(D) 188.5
(E) 201
23. The equation $z(z+i)(z+3 i)=2002 i$ has a zero of the form $a+b i$, where $a$ and $b$ are positive real numbers. Find $a$.
(A) $\sqrt{118}$
(B) $\sqrt{210}$
(C) $2 \sqrt{210}$
(D) $\sqrt{2002}$
(E) $100 \sqrt{2}$
24. Let $A B C D$ be a regular tetrahedron and let $E$ be a point inside the face $A B C$. Denote by $s$ the sum of the distances from $E$ to the faces $D A B, D B C, D C A$, and by $S$ the sum of the distances from $E$ to the edges $A B, B C, C A$. Then $\frac{s}{S}$ equals
(A) $\sqrt{2}$
(B) $\frac{2 \sqrt{2}}{3}$
(C) $\frac{\sqrt{6}}{2}$
(D) 2
(E) 3
25. Let $a$ and $b$ be real numbers such that $\sin a+\sin b=\frac{\sqrt{2}}{2}$ and $\cos a+\cos b=\frac{\sqrt{6}}{2}$. Find $\sin (a+b)$
(A) $\frac{1}{2}$
(B) $\frac{\sqrt{2}}{2}$
(C) $\frac{\sqrt{3}}{2}$
(D) $\frac{\sqrt{6}}{2}$
(E) 1

